# $\mathbf{L n}_{2} \mathbf{M o O}_{6}$-Type Rare Earth Molybdates-Preparation and Lattice Parameters 

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#### Abstract

The title compounds have been prepared for $\mathrm{Ln}=$ rare earth elements $58(\mathrm{Ce})$ through $71(\mathrm{Lu})$ as well as Y and La. They fall into three structural categories: the tetragonal $I 42 \mathrm{~m}$ space group for the large ions up to and including $\mathrm{Sm}_{2} \mathrm{MoO}_{6}$, which can also crystallize in the $C 2 / c$ symmetry found for the small rare earths; and an $\mathrm{Fm} 3 m$ related structure for $\mathrm{Ce}_{2} \mathrm{MoO}_{6}$, which constitutes an exception in the series. Cell parameters are also given for $\mathrm{Gd}_{2} \mathrm{WO}_{6}$ and a series of $\mathrm{Gd}_{2-x} \mathrm{Bi}_{x} \mathrm{MoO}_{6}$ solid solutions.


## Introduction

In conjunction with the ferroelectric $\mathrm{Ln}_{2}$ $\left(\mathrm{MoO}_{4}\right)_{3}$-type rare earth molybdates (1), $\mathrm{Gd}_{2}$ $\mathrm{MoO}_{6}$ has been of interest as an impurity component in single crystals of $\mathrm{Gd}_{2}\left(\mathrm{MoO}_{4}\right)_{3}$. Together with all other rare earth compositions of the same type (except $\mathrm{Ce}_{2} \mathrm{MoO}_{6}$ ) as well as the Y and La compounds, $\mathrm{Gd}_{2} \mathrm{MoO}_{6}$ has been discussed by Blasse (2). The structure of $\mathrm{La}_{2}$ $\mathrm{MoO}_{6}$ has been determined by Sillen (3). Blasse (2) postulated a structure for the small rare earth molybdates based on a monoclinic distortion of the $I \overline{4} 2 m$ symmetry of $\mathrm{La}_{2} \mathrm{MoO}_{6}$. While this appeared to be a reasonable approach, it was not unambiguous, lacking single-crystal data for these monoclinic compositions. We were also unable to index our Guinier patterns using Blasse's (2) parameters. One of the difficulties with the $\mathrm{Ln}_{2} \mathrm{MoO}_{6}$ type rare earth molybdates is the fact that they are highly refractory with melting points in the vicinity of $1600-2000^{\circ} \mathrm{C}$. Such melts are usually dark colored, because of at least a partial loss of oxygen, and would not be suitable for direct crystal growth via the Bridgeman or Czochralski technique. We therefore followed an alternative approach by substituting Bi for Gd in $\mathrm{Gd}_{2} \mathrm{MoO}_{6}$, thereby lowering the melting point. Although the range of existence for the monoclinic structure of these

[^0]solid solutions is rather limited, single crystals of this structure could be obtained by sintering at $1400^{\circ} \mathrm{C}$. Precession work with such single crystals indicated $C 2 / c$ or $C 2$ symmetry, and we were able to accurately index and refine all monoclinic patterns based on these findings.

It is the purpose of this paper to establish the range of the two principal structures, to present precision cell parameters based on least-squares refinement, and to describe $\mathrm{Ce}_{2} \mathrm{MoO}_{6}$ as a new composition. The system $\mathrm{Gd}_{2-x} \mathrm{Bi}_{x} \mathrm{MoO}_{6}$ will also be discussed over a limited range of $x$.

## Experimental

All compounds described in this paper were prepared by standard solid-statc techniques from Kerr-McGee $99.9 \%$ pure rare earth oxides and Molybdenum Company high purity $\mathrm{MoO}_{3}$. Homogenized and pressed pellets were sintered finally in sealed Pt capsules between 1400 and $1600^{\circ} \mathrm{C} . \mathrm{Ce}_{2} \mathrm{MoO}_{6}$ was prepared via:

$$
6 \mathrm{CeO}_{2}+\mathrm{Mo}+2 \mathrm{MoO}_{3} \rightarrow 3 \mathrm{Ce}_{2} \mathrm{MoO}_{6}
$$

in sealed evacuated quartz ampoules. The starting oxide for $\mathrm{Pr}_{2} \mathrm{MoO}_{6}$ was black $\mathrm{Pr}_{6} \mathrm{O}_{11}$ which readily loses its excess oxygen at $1200^{\circ} \mathrm{C}$ as does $\mathrm{Tb}_{4} \mathrm{O}_{7}$, which was used to prepare $\mathrm{Tb}_{2} \mathrm{MoO}_{6}$. All other rare earth oxides are in the true sesquioxide state and were only prefired prior to use.

Small crystals of $\mathrm{Gd}_{1.70} \mathrm{Bi}_{0.30} \mathrm{MoO}_{6}$ were obtained by sintering polycrystalline material of this composition in sealed platinum capsules, fluctuating the temperature between 1400 and $1500^{\circ} \mathrm{C}$. Such crystals were examined by X-ray diffraction using a precession camera with Mo radiation. Powder patterns were obtained with a Hägg Guinier camera using $\mathrm{Cu} K \alpha$ radiation and an internal standard of $\mathrm{KCl}\left(a_{0}=6.2931 \AA\right.$ at $25^{\circ} \mathrm{C}$ ).

## Results and Discussion

Although crystals of $\mathrm{Gd}_{1.70} \mathrm{Bi}_{30} \mathrm{MoO}_{6}$ were twinned, the space group appeared unambiguous as either $C c$ or $C 2 / c$ with $a=16.62 \AA, b=11.23$ $\AA, c=5.45 \AA$, and $\beta=108.6^{\circ}$. This cell satisfactorily indexed the Guinier pattern, and similar cells could be used to index all the monoclinic $\mathrm{Ln}_{2} \mathrm{MoO}_{6}$ phases. The refined cell dimensions are given in Table I.

A body-centered monoclinic cell can also be used to describe this structure. This cell appears to be related to the tetragonal cell found for $\mathrm{Ln}_{2} \mathrm{MoO}_{6}$ phases where Ln is large. Consequently, the dimensions of the body-centered
cell are also given in Table I. Its apparent relationship to the tetragonal cell is:

$$
\begin{aligned}
a_{M} & \sim \sqrt{2} \times a_{T} \\
b_{M} & \sim 2 \sqrt{2} \times a_{T} \\
c_{M} & \sim c_{T} .
\end{aligned}
$$

The most likely relationship of our body-centered cell with Blasse's interpretation is the following:

$$
\begin{aligned}
a_{M} & \sim b_{B} \\
b_{M} & \sim 2 / 3 \times c_{B} \\
c_{M} & \sim 3 \times a_{B} \\
\beta_{M} & \sim 180-\gamma_{B}
\end{aligned}
$$

The tetragonal $I \overline{4} 2 \mathrm{~m}$ structure extends from $\mathrm{La}_{2} \mathrm{MoO}_{6}$ to $\mathrm{Sm}_{2} \mathrm{MoO}_{6}$, and the refined cell dimensions of these phases are also given in Table I. Only $\mathrm{Sm}_{2} \mathrm{MoO}_{6}$ has been prepared in both tetragonal and monoclinic modifications. When prepared at $1400^{\circ} \mathrm{C}, \mathrm{Sm}_{2} \mathrm{MoO}_{6}$ has the tetragonal structure, and when prepared at $900^{\circ} \mathrm{C}$, the monoclinic structure is found. The transition from tetragonal to monoclinic is not merely a distortion because the tetragonal form is readily obtained at room temperature by air quenching. Thus, the transition is slow and

TABLE I
Refined Cell Dimensions, ${ }^{a}$ Space Groups, and Colors of the $\mathrm{Ln}_{2} \mathrm{MoO}_{6}$-Type Rare Earth Molybdates

| Ln | Space group | $a, \AA$ | $b, \AA$ | $c, \AA$ | $\beta,{ }^{\circ}$ | $V, \AA^{3}$ | $c^{\prime}, \AA$ | $\beta^{\prime},{ }^{\circ}$ | Color |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| La | $I 42 m$ | 4.093 |  | 16.017 |  | 268.33 |  |  | White |
| Ce | $F m 3 m$ | $5.578^{b}$ |  |  |  | 173.55 |  |  | Black |
| Pr | $I 42 m$ | 4.030 |  | 15.852 |  | 257.48 |  | Green |  |
| Nd |  | 4.005 |  | 15.813 |  | 253.65 |  | Blue |  |
| Sm |  | 3.963 |  | 15.686 |  | 246.36 |  |  |  |
| Sm | $C 2 / c$ | 5.470 | 11.272 | 15.791 | 90.92 | 973.5 | 16.628 | 108.28 |  |
| Eu |  | 5.439 | 11.218 | 15.735 | 91.01 | 960.0 | 16.558 | 108.16 | White |
| Gd |  | 5.425 | 11.185 | 15.678 | 90.85 | 951.1 | 16.514 | 108.33 | White |
| Tb |  | 5.396 | 11.119 | 15.626 | 90.78 | 937.5 | 16.462 | 108.35 | White |
| Dy |  | 5.371 | 11.071 | 15.573 | 90.78 | 925.9 | 16.542 | 109.72 | Yellow |
| Ho |  | 5.349 | 11.028 | 15.516 | 90.65 | 915.2 | 16.469 | 109.60 | Brown |
| Er | 5.328 | 10.985 | 15.479 | 90.59 | 905.3 | 16.412 | 109.53 | Pink |  |
| Tm |  | 5.310 | 10.933 | 15.419 | 90.48 | 895.1 | 16.266 | 108.57 | White |
| Yb | 5.290 | 10.895 | 15.387 | 90.35 | 886.8 | 16.240 | 108.66 | White |  |
| Lu |  | 5.274 | 10.875 | 15.346 | 90.19 | 880.2 | 16.211 | 108.80 | White |
| Y | 5.351 | 11.022 | 15.510 | 90.67 | 914.7 | 16.466 | 109.63 | White |  |

[^1]

Fig. 1. Cell volume vs. $r^{3}$ for the tetragonal $\mathrm{Ln}_{2} \mathrm{MoO}_{6}$ compounds.
involves some rearrangement of atoms. Attempts to convert $\mathrm{Nd}_{2} \mathrm{MoO}_{6}$ to a monoclinic form by annealing for 60 hr at $600^{\circ} \mathrm{C}$ were unsuccessful. Likewise, attempts to convert $\mathrm{Eu}_{2} \mathrm{MoO}_{6}$ to a tetragonal form by quenching from $1600^{\circ} \mathrm{C}$ were unsuccessful. A sample of $\mathrm{Gd}_{2} \mathrm{MoO}_{6}$ was melted $\left(\sim 2000^{\circ} \mathrm{C}\right)$ with a torch flame and quenched. Its X-ray pattern appeared to be of the $\mathrm{CaF}_{2}$ type with $a=5.40 \AA$; however, the composition of this phase may differ slightly from $\mathrm{Gd}_{2} \mathrm{MoO}_{6}$.

Since the monoclinic modifications are more dense than the tetragonal modifications, we attempted to transform the tetragonal phases by quenching from 65 kbar and $1000^{\circ} \mathrm{C}$. The powder patterns of the products resembled the monoclinic type much more than the tetragonal type, but good indexings were not obtained.

The relationship between the cube of the ionic radii (4) and the cell volumes is given in Fig. 1


Fig. 2. Cell volume vs. $r^{3}$ for the monoclinic $\mathrm{Ln}_{2} \mathrm{MoO}_{6}$ compounds.

TABLE II
Lattice Parameters for the $\mathrm{Gd}_{2-x} \mathrm{Bi}_{x} \mathrm{MoO}_{6}$ System

| $X$ | Composition | Space group | $a, \AA$ | $b, \AA$ | $c, \AA$ | $\beta,{ }^{\circ}$ | $V$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.1 | $\mathrm{Gd}_{1.9} \mathrm{Bi}_{0.1} \mathrm{MoO}_{6}$ | $C 2 / c$ | 16.559 | 11.206 | 5.438 | 108.40 | 957.46 |
| 0.2 | $\mathrm{Gd}_{1 . .8} \mathrm{Bi}_{0.2} \mathrm{MoO}_{6}$ |  | 16.59 | 11.218 | 5.447 | 108.523 | 961.72 |
| 0.3 | $\mathrm{Gd}_{1.7} \mathrm{Bi}_{0.3} \mathrm{MoO}_{6}$ |  | 16.624 | 11.227 | 5.452 | 108.61 | 964.33 |
| 0.4 | $\mathrm{Gd}_{1.6} \mathrm{Bi}_{0.4} \mathrm{MoO}_{6}$ | $I 42 m$ | 3.941 | - | 15.690 | - | 243.67 |
| 0.5 | $\mathrm{Gd}_{1.5} \mathrm{BiO}_{0.5} \mathrm{MoO}_{6}$ |  | 3.946 | - | 15.719 | - | 244.73 |
| 0.6 | $\mathrm{Gd}_{1.6} \mathrm{Bi}_{0.4} \mathrm{MoO}_{6}$ |  | 3.948 | - | 15.738 | - | 245.32 |

TABLE III
Observed and Calculated $d$ Values for $\mathbf{G d}_{2} \mathbf{M o O}_{6}$

| $I$ | hkl | $d$ (obs) | $d$ (calc) |
| :---: | :---: | :---: | :---: |
| 10 | 110 | 9.068 | 9.104 |
| 10 | 200 | 7.813 | 7.837 |
| 10 | 310 | 4.723 | 4.734 |
| 5 | 111 | 4.160 | 4.167 |
| 15 | -311 | 4.114 | 4.118 |
| 10 | 130 | 3.623 | 3.627 |
| 100 | 221 | 3.137 | 3.138 |
| 100 | -421 | 3.105 | 3.106 |
| 10 | 330 | 3.033 | 3.034 |
| 5 | 510 | 3.018 | 3.018 |
| 20 | -331 | 2.851 | 2.852 |
| 70 | 040 | 2.794 | 2.796 |
| 65 | -202 | 2.710 | 2.712 |
| 60 | 600 | 2.612 | 2.612 |
| 5 | 421 | 2.453 | 2.454 |
| 10 | 331 | 2.427 | 2.427 |
| 2 | 530 | 2.403 | 2.399 |
| 5 | 022 | 2.339 | 2.338 |
| 5 | 511 | 2.314 | 2.316 |
| 5 | 241 | 2.249 | 2.250 |
| 2 | -441 | 2.239 | - 2.238 |
| 15 | 150 | 2.214 | 2.214 |
| 10 | -332 | 2.168 | 2.168 |
| 10 | 350 | 2.056 | 2.056 |
| 2 | 312 | 2.031 | 2.031 |
| 20 | -712 | 2.003 | 2.003 |
| 10 | -731 | 1.982 | 1.982 |
| 5 | 800 | 1.957 | 1.959 |
| 80 | -242 | 1.946 | 1.946 |
| 75 | 640 | 1.909 | 1.909 |
| 60 | 402 | 1.895 | 1.895 |
| 40 | -802 | 1.868 | 1.867 |
| 15 | -551 | 1.824 | 1.824 |
| 5 | -732 | 1.787 | 1.787 |
| 10 | -113 | 1.745 | 1.745 |
| 10 | -513 | 1.734 | 1.734 |
| 15 | -152 | 1.717 | 1.717 |
| 5 | -423 | 1.707 | 1.707 |
| 50 | 261 | 1.672 | 1.672 |
| 45 | -461 | 1.668 | 1.668 |
| 15 | -931 | 1.646 | 1.645 |
| 50 | 023 | 1.641 | 1.640 |
| 36 | -623 | 1.627 | 1.627 |
| 2 | -713 | 1.614 | 1.615 |
| 45 | -133 | 1.596 | 1.597 |
| 15 | -533 | 1.588 | 1.588 |
| 40 | $-1021$ | 1.584 | 1.583 |
| 40 | 442 | 1.569 | 1.569 |
| 10 | -932 | 1.557 | 1.557 |
| 25 | -842 | 1.553 | 1.553 |
| 10 | 062 | 1.510 | 1.509 |
| 10 | -752 | 1.505 | 1.505 |
| 10 | -371 | 1.503 | 1.503 |

for the tetragonal and in Fig. 2 for the monoclinic compounds.
To attempt to distinguish between the possible centrosymmetric $C 2 / c$ and the noncentrosymmetric $C 2$ space groups, we examined some $\mathrm{Gd}_{1.8} \mathrm{Bi}_{0.2} \mathrm{MoO}_{6}$ crystals for their piezoelectric response by the transmission method (5). As this test was negative, it tended to support the $C 2 / c$ space group. A more unambiguous distinction between the two possibilities was made by a second harmonic generation (SHG) test with the same compound. Since this test was also negative, we assume that $C 2 / c$ is the correct space group.

Many $\mathrm{Ln}_{2} \mathrm{WO}_{6}$ tungstates have the same structure found for the monoclinic $\mathrm{Ln}_{2} \mathrm{MoO}_{6}$ phases. For example, we find the refined bodycentered cell dimensions of $\mathrm{Gd}_{2} \mathrm{WO}_{6}$ to be $a=5.425 \AA, b=11.172 \AA, c=15.624 \AA, \beta=$ $91.60^{\circ}$, and $V=946.7 \AA^{3}$. This series constitutes one of the rare cases where the cell volumes of the tungstates are actually smaller than those of the corresponding isostructural molybdates. Precision cell edges of the remaining $\mathrm{Ln}_{2} \mathrm{WO}_{6}$ compounds will be the subject of a forthcoming


Fig. 3. Log resistivity vs. inverse temperature for $\mathrm{Ce}_{2} \mathrm{MoO}_{6}$.
publication. The cell dimensions and space group for the $\mathrm{Gd}_{2-x} \mathrm{Bi}_{x} \mathrm{MoO}_{6}$ system over a limited region of $x$ are summarized in Table II. Table III gives the observed and calculated $d$ spacings for $\mathrm{Gd}_{2} \mathrm{MoO}_{6}$ using the $C$-centered cell.

While there appears to be no question as to the valence state of the rare earths in most of these compositions, it is not quite clear in $\mathrm{Ce}_{2} \mathrm{MoO}_{6}$. Since the compound is black and a semiconductor, we are assuming at this point that a variable valence distribution such as $\mathrm{Ce}^{3+} \mathrm{Ce}^{4+} \mathrm{Mo}^{5+} \mathrm{O}_{6}$ is responsible for this behavior. It is also probable that this different distribution of valence states is responsible for the different structure observed for this compound. It is interesting to note that $\mathrm{Ce}^{3+}$ and $\mathrm{Mo}^{6+}$ are apparently compatible in a $1: 1.5$ ratio in a compound such as $\mathrm{Ce}_{2}^{3+}\left(\mathrm{Mo}^{6+} \mathrm{O}_{4}\right)_{3}$ (which is transparent, yellow, and an insulator) while the $2: 1$ ratio in $\mathrm{Ce}_{2} \mathrm{MoO}_{6}$ did cause a reduction of $\mathrm{Mo}^{6+}$ to $\mathrm{Mo}^{5+}$. A typical resistivity vs. tempera-
ture plot is given in Fig. 3. The calculated activation energy is .21 eV .

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[^0]:    * Contribution No. 1878.

[^1]:    ${ }^{a}$ The unprimed values refer to the body-centered cell, and the primed values to the C -centered cell where $c^{\prime}=a$ and $b^{\prime}=b$. The $4-5 \AA$ edges are accurate to $\pm .001 \AA$, the $10-11 \AA$ edges to $\pm .002 \AA$, and the $15-16 \AA$ to $\pm .003 \AA$.
    ${ }^{b}$ This cell edge and space group only represents a subcell.

